

Verification and Validation of a Three-Dimensional Generalized Composite Material Model

Canio Hoffarth, Joseph Harrington and Subramaniam D. Rajan

School of Sustainable Engineering and the Built Environment, Arizona State University, Tempe, AZ

Robert K. Goldberg and Kelly S. Carney

NASA-GRC, Cleveland, OH

Paul Du Bois

George Mason University, Fairfax, VA

Gunther Blankenhorn

LSTC, Livermore, CA

Abstract

A general purpose orthotropic elasto-plastic computational constitutive material model has been developed to accurately predict the response of composites subjected to high velocity impact. The three-dimensional orthotropic elasto-plastic composite material model is being implemented initially for solid elements in LS-DYNA[®] as MAT213. In order to accurately represent the response of a composite, experimental stress-strain curves are utilized as input, allowing for a more general material model that can be used on a variety of composite applications. The theoretical details are discussed in a companion paper. This paper documents the implementation, verification and validation of the material model using the T800-F3900 fiber/resin composite material.

Introduction

Composite materials are now beginning to provide uses hitherto reserved for metals in structural systems such as airframes and engine containment systems, wraps for repair and rehabilitation and ballistic/blast mitigation systems. While material models exist that can be used to simulate the response of the materials in these demanding structural systems, they are often designed for use with specific materials such as metals [1] [2], polymers [3] and wood [4]. Most are tailored specifically for an application and have limitations - purely elastic, no rate sensitivity, implementation for solid elements only, and limited damage and failure characterization [5]-[10].

A few examples of different approaches to composite damage modeling include Littell et al. [11], Matzenmiller et al. [12], and others [13]-[18]. Yen's comprehensive model [19] is implemented in LS-DYNA as *MAT_162. Availability of constitutive models for composite materials in LS-DYNA is discussed in some length in our companion paper [20] and that explains the motivation for this study.

In the next section we briefly discuss the theoretical development of the constitutive model. This is followed by details of the numerical algorithm, verification tests for a composite used in the

aerospace industry, the use of the composite in a high speed contact example and finally, concluding remarks including details of our ongoing and future work.

Orthotropic 3D Elasto-Plastic Composite Material Model

The material law that the model is built upon describes the elastic and permanent deformation of the composite with full three-dimensional implementation suitable for solid elements. Only the relevant equations used in the numerical algorithm are presented here. The theoretical basis and discussions are available in a companion paper [20]. Current development of the model includes complete elasto-plastic deformation model, with damage and failure to be added later.

The Tsai-Wu surface is used as the yield surface for the plasticity model and is defined as

$$f(\sigma) = a + (F_1 \ F_2 \ F_3 \ 0 \ 0 \ 0) \begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{12} \\ \sigma_{23} \\ \sigma_{31} \end{bmatrix} + \begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{12} \\ \sigma_{23} \\ \sigma_{31} \end{bmatrix}^T \begin{bmatrix} F_{11} & F_{12} & F_{13} & 0 & 0 & 0 \\ F_{12} & F_{22} & F_{23} & 0 & 0 & 0 \\ F_{13} & F_{23} & F_{33} & 0 & 0 & 0 \\ 0 & 0 & 0 & F_{44} & 0 & 0 \\ 0 & 0 & 0 & 0 & F_{55} & 0 \\ 0 & 0 & 0 & 0 & 0 & F_{66} \end{bmatrix} \begin{bmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{12} \\ \sigma_{23} \\ \sigma_{31} \end{bmatrix} \quad (1)$$

where $a = -1$ and

$$\begin{aligned} F_1 &= \frac{1}{\sigma_{11}^T} - \frac{1}{\sigma_{11}^C} & F_{11} &= \frac{1}{\sigma_{11}^T \sigma_{11}^C} & F_{44} &= \frac{1}{\sigma_{12}^2} \\ F_2 &= \frac{1}{\sigma_{22}^T} - \frac{1}{\sigma_{22}^C} & F_{22} &= \frac{1}{\sigma_{22}^T \sigma_{22}^C} & F_{55} &= \frac{1}{\sigma_{23}^2} \\ F_3 &= \frac{1}{\sigma_{33}^T} - \frac{1}{\sigma_{33}^C} & F_{33} &= \frac{1}{\sigma_{33}^T \sigma_{33}^C} & F_{66} &= \frac{1}{\sigma_{31}^2} \\ F_{ij} &= \frac{2}{(\sigma_{45}^{i-j})^2} - \frac{F_i + F_j}{\sigma_{45}^{i-j}} - \frac{1}{2}(F_{ii} + F_{jj} + F_{kk}) & & & & i, j = 1, 2, 3, k = i + 3 \end{aligned} \quad (1a)$$

The stress components of the yield function coefficients correspond to the yield stresses associated with each experimental curve, which vary with the effective plastic strain, thus allowing the model to describe different hardening properties in each direction. The non-associative flow surface is defined as

$$h = \sqrt{H_{11}\sigma_{11}^2 + H_{22}\sigma_{22}^2 + H_{33}\sigma_{33}^2 + 2H_{12}\sigma_{11}\sigma_{22} + 2H_{23}\sigma_{22}\sigma_{33} + 2H_{31}\sigma_{33}\sigma_{11} + H_{44}\sigma_{12}^2 + H_{55}\sigma_{23}^2 + H_{66}\sigma_{31}^2} \quad (2)$$

where the H_{ij} terms are the constant flow rule coefficients. The rest of the details can be found in the companion paper [20].

The first six flow rule coefficients are computed directly from the assumed flow rule coefficient value and the plastic Poisson's ratios.

$$\begin{aligned} H_{12} &= -\nu_{12}^p H_{11} & H_{23} &= \frac{-\nu_{23}^p \nu_{12}^p}{\nu_{21}^p} H_{11} \\ H_{13} &= -\nu_{13}^p H_{11} & & & & \\ H_{22} &= \frac{\nu_{12}^p}{\nu_{21}^p} H_{11} & H_{33} &= \frac{\nu_{13}^p}{\nu_{31}^p} H_{11} \end{aligned} \quad (3a)$$

The last three flow rule coefficients (H_{44} , H_{55} , H_{66}) are calculated iteratively with the user-defined range to best fit the shear curves. For example, to determine H_{44} , the following optimization problem is posed using the input curve for the “1-2” shear case.

Find H_{44} to minimize

$$f(H_{44}) = \sum_{i=1}^n \left[(\hat{\sigma}_{22})_i - (\hat{\sigma}_{12})_i \right]^2 \quad (3b)$$

such that

$$H_{44}^{\min} \leq H_{44} \leq H_{44}^{\max} \quad (3c)$$

where n is the number of data points on the master curve, $(\hat{\sigma}_{22})_i$ is the i^{th} effective stress value from the master curve, and $(\hat{\sigma}_{12})_i$ is the effective stress value for the shear curve using an assumed value of H_{44} .

Numerical Algorithm

In this initial implementation, we do not account for rate and temperature dependency, damage accumulation and failure. The following experimental data are needed as LS-DYNA input.

- (1) A total of 12 true stress versus true strain curves under quasi-static test conditions from (a) uniaxial tension in 1, 2 and 3-directions, (b) uniaxial compression in 1, 2 and 3-directions, (c) shear in 1-2, 2-3 and 3-1 planes and (d) off-axis (e.g. 45 degrees) uniaxial tension or compression in 1-2, 2-3 and 3-1 planes. The tabulated x-y data for each curve is read in and used appropriately.
- (2) The elastic modulus of elasticity, Poisson’s ratio and average plastic Poisson’s ratio obtained from the tension and compression tests.

The effective plastic strain can be written in terms of the experimental stress versus total strain data. In the 1-direction for example, this is written as

$$\left. \begin{aligned} \sigma_{11}^c \left(\varepsilon_{11}^p = \varepsilon_{11} - \frac{\sigma_{11}^c}{E_{11}} \right) \\ \varepsilon_e^p = \int (\sigma_{11} d\varepsilon_{11}^p / h) \end{aligned} \right\} \Rightarrow \sigma_{11}^c(\varepsilon_e^p) \quad (4)$$

where σ_{11}^c is the experimental compressive true stress in the 1-direction, ε_{11} is the total true strain in the 1-direction, E_{11} is the elastic modulus in the 1-direction, ε_{11}^p is the true plastic strain in the x-direction, ε_e^p is the effective plastic strain and h is the flow rule value, which is equivalent to the effective stress, shown in Eqn. (2). The material model uses a typical elastic stress update as

$$\boldsymbol{\sigma}^{n+1} = \boldsymbol{\sigma}^n + \mathbf{C}\Delta t : (\dot{\boldsymbol{\varepsilon}} - \dot{\boldsymbol{\varepsilon}}^p) \quad (5)$$

where \mathbf{C} is the orthotropic constitutive matrix, Δt is the time step, $\dot{\boldsymbol{\varepsilon}}$ is the total strain rate and $\dot{\boldsymbol{\varepsilon}}^p$ is the plastic strain rate. The constitutive matrix is written in terms of the compliance matrix as

$$\mathbf{C} = \mathbf{S}^{-1} = \begin{bmatrix} \frac{1}{E_{11}} & -\frac{\nu_{21}}{E_{22}} & -\frac{\nu_{31}}{E_{33}} & 0 & 0 & 0 \\ & \frac{1}{E_{22}} & -\frac{\nu_{32}}{E_{33}} & 0 & 0 & 0 \\ & & \frac{1}{E_{33}} & 0 & 0 & 0 \\ & & & \frac{1}{G_{23}} & 0 & 0 \\ & Sym & & & \frac{1}{G_{31}} & 0 \\ & & & & & \frac{1}{G_{12}} \end{bmatrix}^{-1} \quad (7)$$

where E is the elastic modulus in the principal material directions, G is the elastic shear modulus and ν is the elastic Poisson's ratio. The yield stresses used to determine the flow rule coefficients are summarized into a single vector, corresponding to each of the experimental test curves as $\mathbf{q}^T = [\sigma_{11}^T \ \sigma_{22}^T \ \sigma_{33}^T \ \sigma_{11}^C \ \sigma_{22}^C \ \sigma_{33}^C \ \sigma_{12} \ \sigma_{23} \ \sigma_{31} \ \sigma_{45-12}^C \ \sigma_{45-23}^C \ \sigma_{45-31}^C]$. Lastly, the consistency condition is written in terms of the rate of yield function as

$$\dot{f} = \frac{\partial f}{\partial \boldsymbol{\sigma}} \dot{\boldsymbol{\sigma}} + \frac{\partial f}{\partial \mathbf{q}} \dot{\mathbf{q}} = 0 \quad (8)$$

which is defined as a non-associative flow with strain hardening (hence the inclusion of the yield stress vector). Eqn. (8) can be expanded as

$$\dot{f} = \frac{\partial f}{\partial \boldsymbol{\sigma}} \left(\mathbf{C} : \dot{\boldsymbol{\epsilon}} - \mathbf{C} : \dot{\lambda} \frac{\partial h}{\partial \boldsymbol{\sigma}} \right) + \frac{\partial f}{\partial \mathbf{q}} \dot{\lambda} \frac{d\mathbf{q}}{d\lambda} = 0 \quad (9)$$

where $\dot{\boldsymbol{\sigma}}$ is written in terms of the constitutive matrix and strain rates. Solving for the effective plastic strain rate produces the following equation.

$$\dot{\lambda} = \frac{\frac{\partial f}{\partial \boldsymbol{\sigma}} \mathbf{C} : \dot{\boldsymbol{\epsilon}}}{\frac{\partial f}{\partial \boldsymbol{\sigma}} \mathbf{C} : \frac{\partial h}{\partial \boldsymbol{\sigma}} + \frac{\partial f}{\partial \mathbf{q}} \frac{d\mathbf{q}}{d\lambda}} \quad (10)$$

Initially, a perfectly elastic response is assumed. Thus, an elastic predictor is used to compute the stresses as

$$\begin{aligned} (\sigma_{11})^e &= (\sigma_{11})^n + C_{11}\Delta t(\dot{\epsilon}_{11}) + C_{12}\Delta t(\dot{\epsilon}_{22}) + C_{13}\Delta t(\dot{\epsilon}_{33}) \\ (\sigma_{22})^e &= (\sigma_{22})^n + C_{12}\Delta t(\dot{\epsilon}_{11}) + C_{22}\Delta t(\dot{\epsilon}_{22}) + C_{23}\Delta t(\dot{\epsilon}_{33}) \\ (\sigma_{33})^e &= (\sigma_{33})^n + C_{13}\Delta t(\dot{\epsilon}_{11}) + C_{23}\Delta t(\dot{\epsilon}_{22}) + C_{33}\Delta t(\dot{\epsilon}_{33}) \\ (\sigma_{12})^e &= (\sigma_{12})^n + C_{44}\Delta t(\dot{\epsilon}_{12}) \\ (\sigma_{23})^e &= (\sigma_{23})^n + C_{55}\Delta t(\dot{\epsilon}_{23}) \\ (\sigma_{31})^e &= (\sigma_{31})^n + C_{66}\Delta t(\dot{\epsilon}_{31}) \end{aligned} \quad (11)$$

With the elastic trial stresses computed, a trial yield function value can be calculated and used to determine if the load step is elastic or plastic. It should be noted that the elastic trial stress is used as the stress in the next step if the trial yield function value is less than or equal to zero. Otherwise, the stress state is beyond the yield surface and must be brought back using a radial return and plastic corrector, $\Delta\lambda$. If the trial yield function happens to be greater than zero, then $\Delta\lambda > 0$ must be true. The value of $\Delta\lambda$ is determined using a secant iteration, with $\Delta\lambda^1 = 0$ for the first iteration and the second value for the increment of the plastic multiplier determined from consistency,

$$\Delta\lambda^2 = \frac{\frac{\partial f}{\partial \boldsymbol{\sigma}} \Big|_e : (\boldsymbol{\sigma}^e - \boldsymbol{\sigma}^n)}{\frac{\partial f}{\partial \boldsymbol{\sigma}} \Big|_e \mathbf{C} : \frac{\partial h}{\partial \boldsymbol{\sigma}} \Big|_e + \frac{\partial f}{\partial \mathbf{q}} \frac{d\mathbf{q}}{d\lambda}} \approx \frac{\frac{\partial f}{\partial \boldsymbol{\sigma}} \Big|_e : (\boldsymbol{\sigma}^e - \boldsymbol{\sigma}^n)}{\frac{\partial f}{\partial \boldsymbol{\sigma}} \Big|_e \mathbf{C} : \frac{\partial h}{\partial \boldsymbol{\sigma}} \Big|_e} \quad (12)$$

where the derivatives of \mathbf{q} are taken as zero, meaning that the response is perfectly plastic. The initial calculation of the second increment corresponds to perfect plasticity in order to ensure that the stress state returns to the interior of the yield surface, resulting in a negative value of the yield function and bounding the solution. From each estimate of $\Delta\lambda$, the corresponding corrected stresses can be computed as well as the yield stresses obtained from the input stress versus effective plastic strain (λ) data. With these terms calculated for both estimates of $\Delta\lambda$, the yield function value for each can be computed with the third estimate evaluated as

$$\Delta\lambda^3 = \Delta\lambda^1 - f^1 \frac{\Delta\lambda^2 - \Delta\lambda^1}{f^2 - f^1} \quad (13)$$

The corrected stresses and yield stresses associated with $\Delta\lambda^3$ are then calculated and used to obtain a new estimate of the yield function value. Convergence of the secant iteration is determined by the following conditions

$$f_3 > 0 \Rightarrow \begin{cases} \Delta\lambda^1 = \Delta\lambda^3 \\ \Delta\lambda^2 = \Delta\lambda^2 \end{cases}; \quad f_3 < 0 \Rightarrow \begin{cases} \Delta\lambda^1 = \Delta\lambda^1 \\ \Delta\lambda^2 = \Delta\lambda^3 \end{cases}; \quad f_3 \approx 0 \Rightarrow \Delta\lambda = \Delta\lambda^3 \quad (14)$$

with the secant iteration continuing if the new yield function value is not less than some defined tolerance. Once convergence is met, the plastic multiplier increment to return the stress state to the yield surface is known and the stresses can be updated as

$$\boldsymbol{\sigma}^{n+1} = \boldsymbol{\sigma}^e - \mathbf{C} : \Delta\lambda \frac{\partial h}{\partial \boldsymbol{\sigma}} \Big|_e \quad (15)$$

Finally, the yield stresses are updated as well, using the new value of the overall effective plastic strain, λ , in each input curve to determine the corresponding yield stress level as

$$q^{n+1} = q(\lambda^n + \Delta\lambda^3) \quad (16)$$

This results in anisotropic strain hardening, as a yield stress increase in each direction is initiated with plasticity in any direction, but at different levels. A detailed algorithm is presented below.

Step 1: Preprocessing

- Convert stress/strain input curves to stress versus effective plastic strain using Eqn. (4).
- Store initial yield stresses in \mathbf{q} .
- Calculate and store the elastic moduli from the initial yield stress and strain values.
- Store the three elastic Poisson's ratio values and flow rule coefficients from input.
- Compute optimal values of the flow rule coefficients so as to match the input curves as closely as possible.

Step 2: Initialization

Parameters available at start of step: $\mathbf{q}_n, \boldsymbol{\sigma}_n, (\dot{\boldsymbol{\epsilon}}_n, \Delta t_n) \rightarrow \Delta \boldsymbol{\epsilon}_n, \lambda_n$.

Step 3: Elastic predictor

Compute and set the yield function coefficients using Eqn. (1a).

Construct the constitutive matrix using Eqn. (7).

Compute elastic trial stresses, $\boldsymbol{\sigma}_{n+1}^e$, using Eqn. (11).

Compute the trial yield function, f_{n+1}^{trial} , using the elastic trial stresses in Eqn. (1).

If $f_{n+1}^{trial} \leq 0$, the elastic solution is correct, set $\Delta \lambda_n = 0$ and go to stress update. Else go to plastic corrector.

Step 4: Plastic corrector

Set $\Delta \lambda^1 = 0$.

Calculate $\Delta \lambda^2$ from Eqn. (12).

Loop through secant iteration for specified max number of iterations:

Compute the new estimate of the stress for each plastic multiplier increment $(\Delta \lambda^1, \Delta \lambda^2)$ using Eqn. (15).

Calculate the effective plastic strains (λ^1, λ^2) at the next time step using the estimates of the plastic multiplier increment; then obtain the strain hardening parameters with the effective plastic strain from the curve data (true plastic stress as a function of effective plastic strain).

Compute new plastic multiplier increment, $\Delta \lambda^3$. Calculate new estimate for the yield function, f^3 . If $|f^3| \leq tol$, set $\Delta \lambda = \Delta \lambda^3$, exit the loop and go to stress update. Else update secant iteration parameters using Eqn. (14) and go to next step of secant iteration.

Step 5: Stress Update

Calculate $\boldsymbol{\sigma}_{n+1}$ using Eqn. (15).

Step 6: Update history variables for plastic work and work hardening parameters (\mathbf{q} and λ)

Set $\lambda_{n+1} = \lambda_n + \Delta \lambda_n$.

Determine new yield stresses, \mathbf{q}_{n+1} , using λ_{n+1} and Eqn. (16).

Model Verification

The composite material model was tested and verified using experimental data obtained from T800S/3900-2B [P2352W-19] BMS8-276 Rev-H-Unitape fiber/resin unidirectional composite [21]. Toray describes T800S as an intermediate modulus, high tensile strength graphite fiber. The epoxy resin system is labeled F3900 where a toughened epoxy is combined with small elastomeric particles to form a compliant interface or interleaf between fiber plies to resist impact damage and delamination [22]. Magnified views of the composite are shown in Figs. 1 and 2.

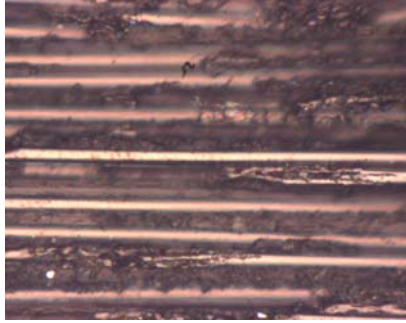


Fig. 1. Side view obtained using optical microscopy

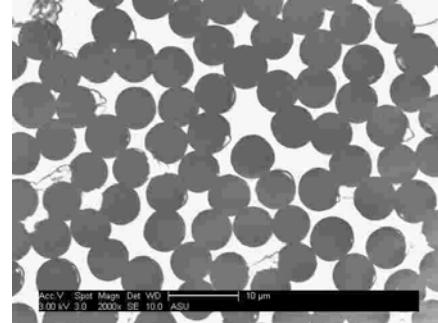


Fig. 2 Logitudinal view obtained using a SEM

The source of the input data for the model (both experimental and virtual) is listed Table 1. In the *Data* column, *Experimental* refers to experimental data generated at Wichita State [21], and *MAC-GMC* [23] and *VTSS* [24] refer to the use of numerical simulation techniques to generate the stress-strain curve when experimental data are not available.

Table 1. Generation of input data for T800-F3900 composite

Curve	Data
Tension Test (1-Direction)	Experimental
Tension Test (2-Direction)	MAC-GMC and VTSS
Tension Test (3-Direction)	Transverse isotropy
Compression Test (1-Direction)	Experimental
Compression Test (2-Direction)	MAC-GMC and VTSS
Compression Test (3-Direction)	Transverse isotropy
Pure Shear Test (1-2 Plane)	Experimental
Pure Shear Test (2-3 Plane)	MAC-GMC and VTSS
Pure Shear Test (1-3 Plane)	Transverse isotropy
Off-Axis Test (45°, 1-2 Plane)	MAC-GMC and VTSS
Off-Axis Test (45°, 2-3 Plane)	MAC-GMC and VTSS
Off-Axis Test (45°, 1-3 Plane)	Transverse isotropy

The fiber (transversely isotropic, linear elastic) and the matrix (isotropic, elasto-plastic) properties are listed in Table 2. The properties for the latter are not publicly available. Hence they were assumed as shown in the table.

Table 2. T800-F3900 fiber and matrix properties (Volume Fraction = 0.54)

Property	Fiber	Matrix
E_1 , psi	$4(10^7)$	$5(10^5)$
E_2 , psi	$2.25(10^7)$	
E_3 , psi	$2.25(10^7)$	
ν_{12}	0.2	0.35
ν_{23}	0.25	
ν_{13}	0.25	
G , psi	$1.5(10^7)$	$1.85(10^5)$
σ_y , psi		$2(10^4)$

Results from the preprocessing step in terms of computing the optimal flow-rule coefficients (solution to Eqns. (3b) and (3c)) are shown in Figs. 3 and 4.

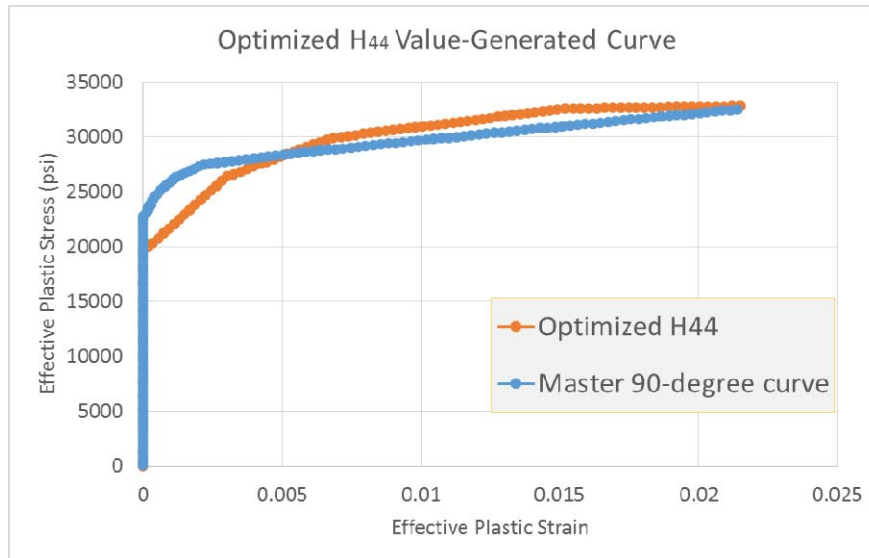


Fig. 3. Comparison of master curve with optimized H₄₄ (and H₆₆) value

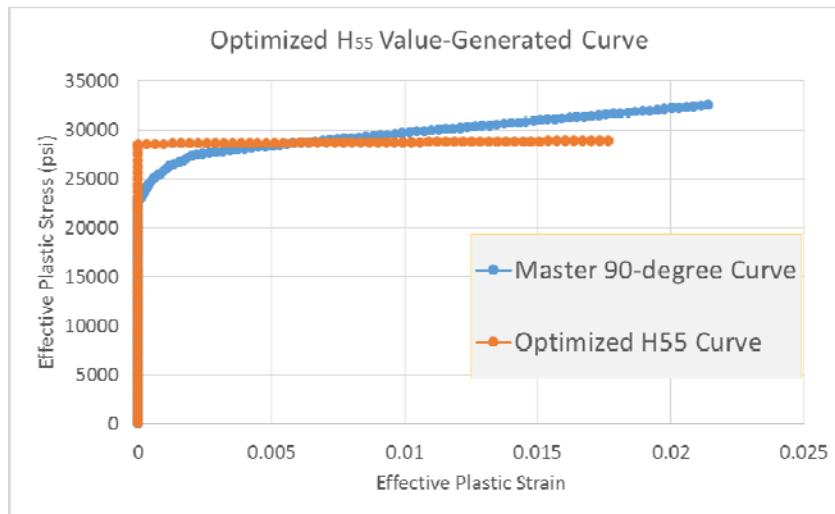


Fig. 4 Comparison of master curve with optimized H₅₅ value

With the computed data so far, the verification process can be executed. Schematics for the tension and compression tests are shown in Fig. 55 and Fig. 66, respectively.

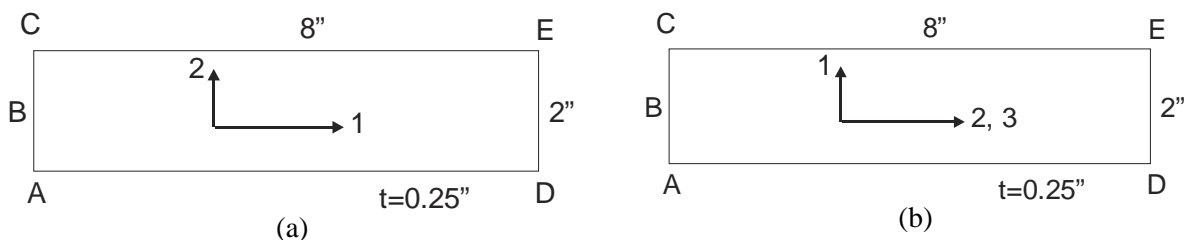


Fig. 5. Schematics for tension test cases (a) 1-direction (b) 2 and 3-directions

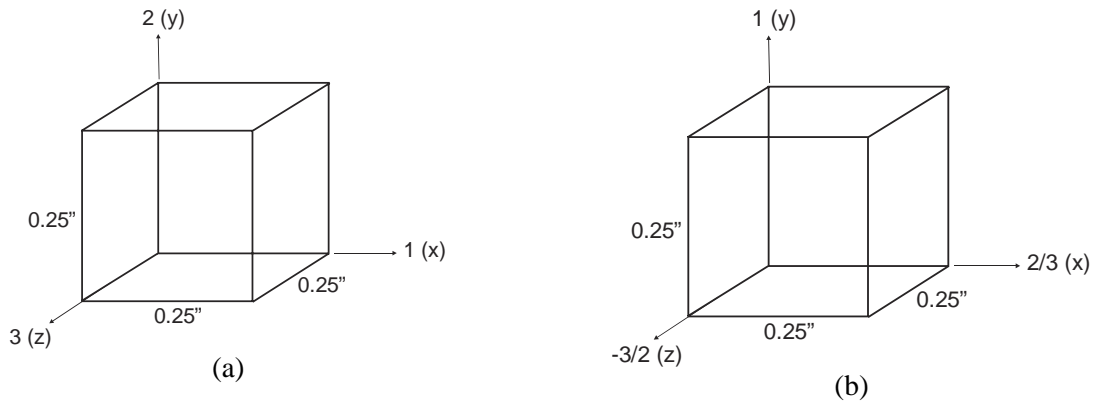


Fig. 6. Schematics for compression test cases (a) 1-direction (b) 2 and 3-directions

The simulations for the tension and compression tests in all directions were executed using different mesh sizes ranging from 1 element to 64 elements. 64-element meshes for the tension and compression test cases are shown in Fig. 77 and Fig. 8, respectively.

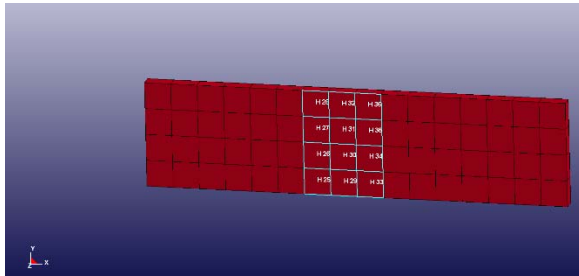


Fig. 7. 64-element mesh for tension test cases

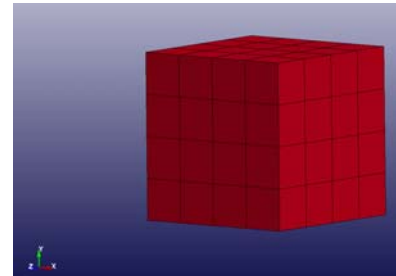
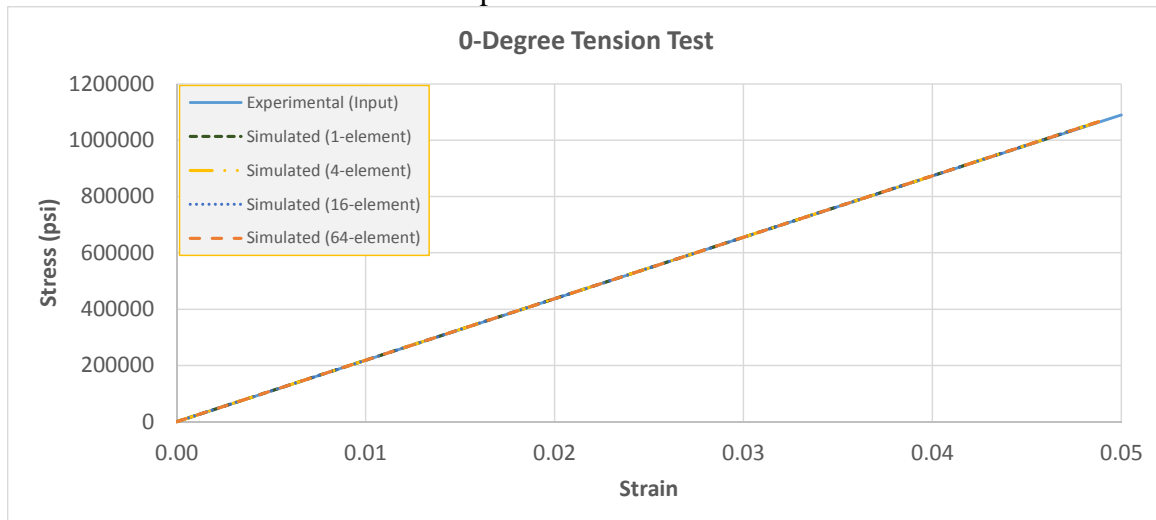
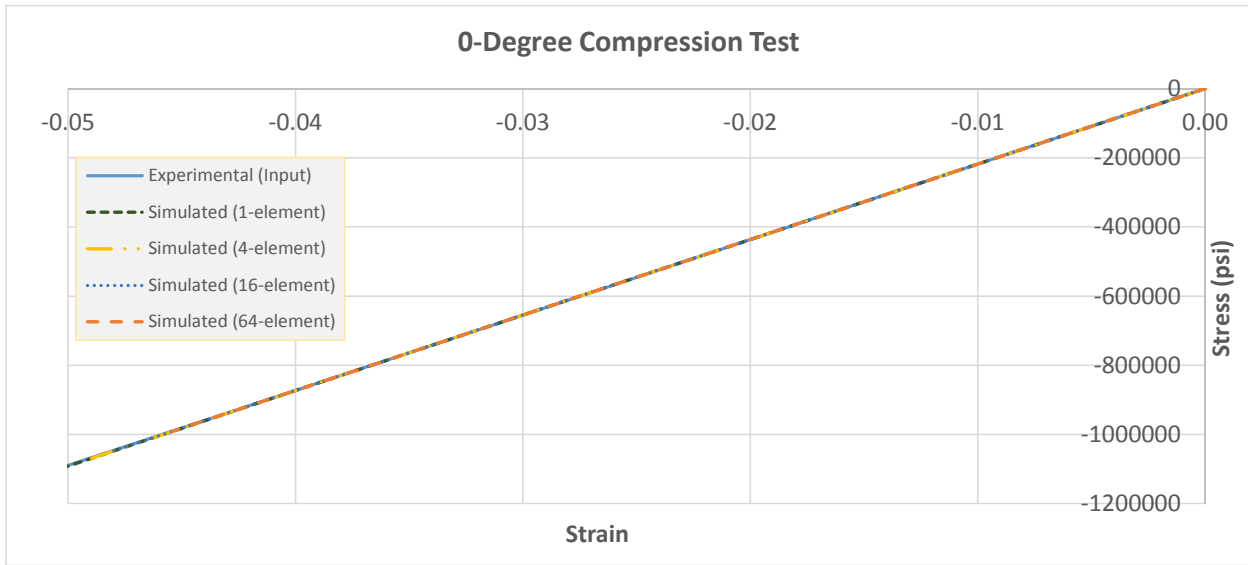


Fig. 8. 64-element mesh for compression test cases

For both tension and compression tests, nodes on face ABC were constrained in the x-direction and the center node was also constrained in the y-direction. A 0.5 in/s displacement in the x-direction was applied to all the nodes on the right face, E-D. For the compression tests, care was taken to ensure that the model yielded but did not buckle. The simulated and experimental stress-strain curves for the tension and compression tests are shown in



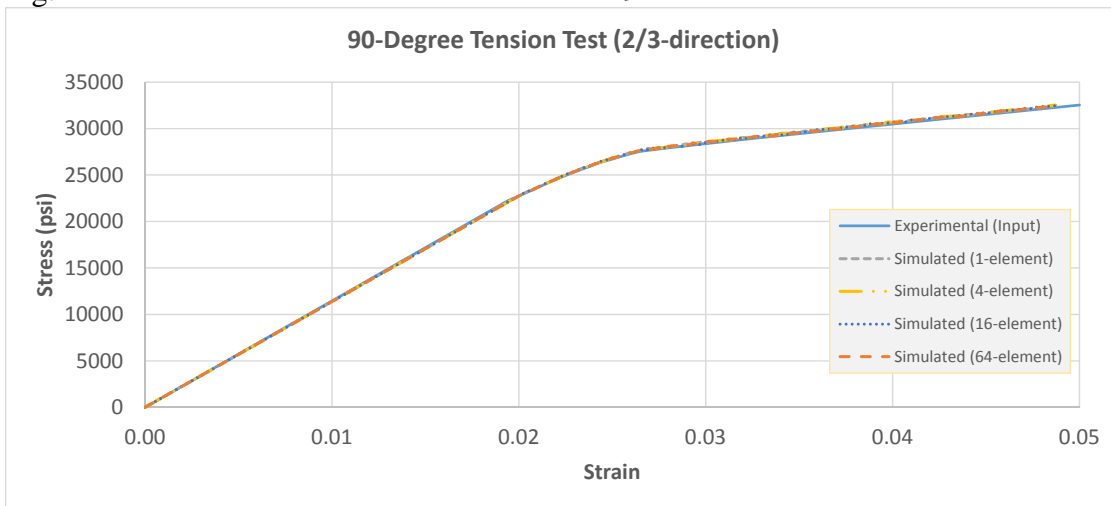
(a)



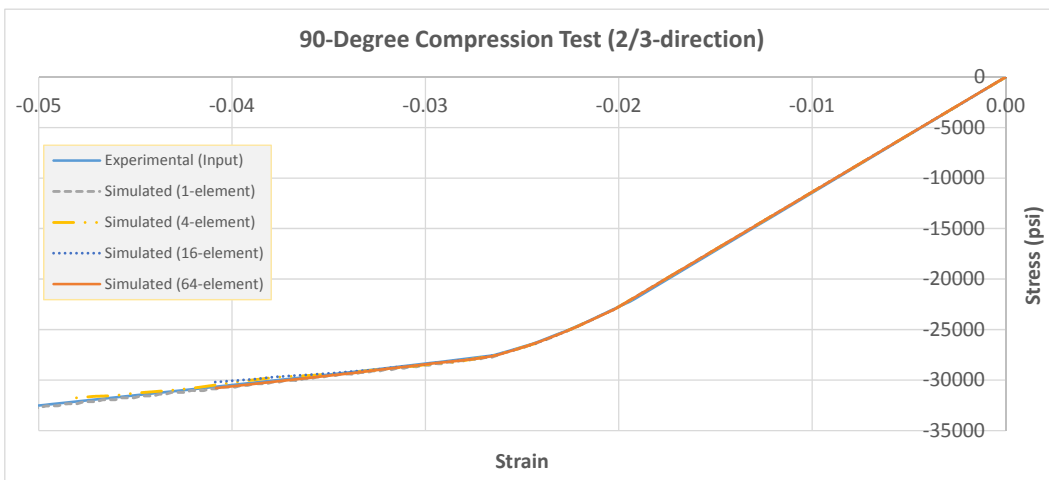
(b)
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Fig.

and

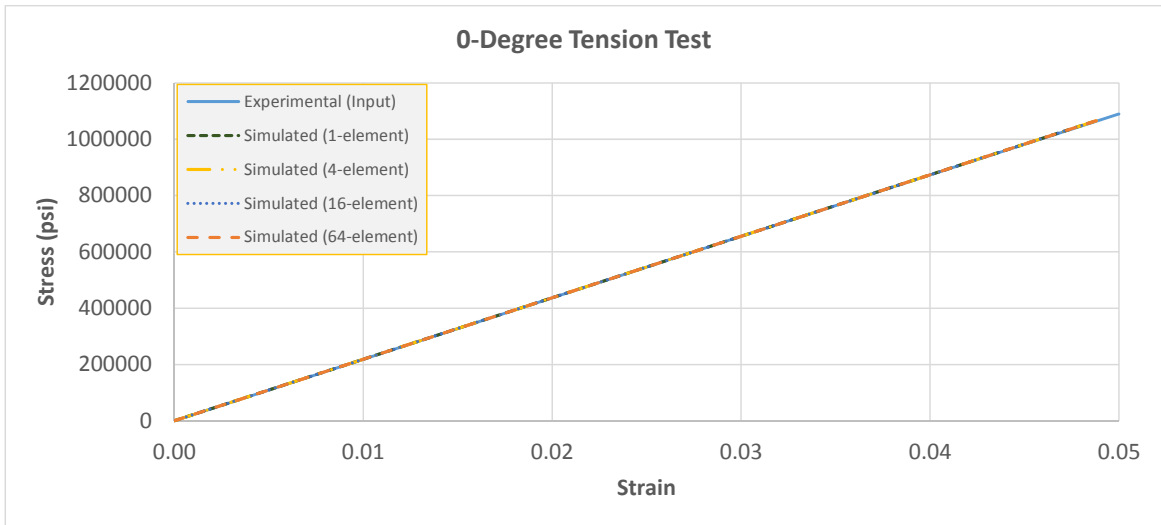


(a)

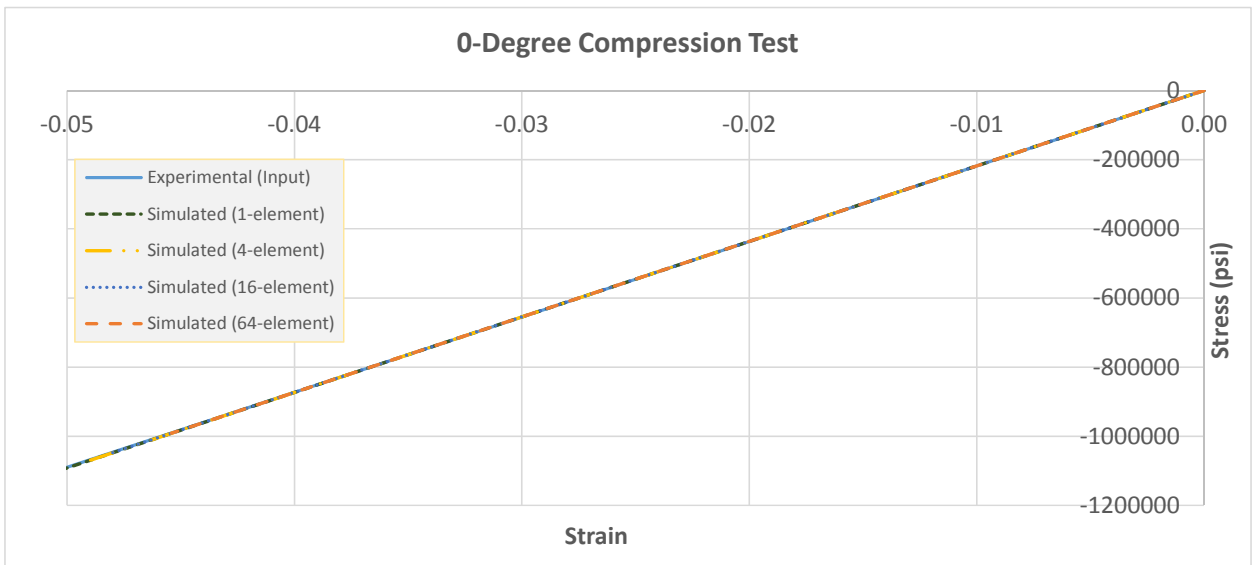


(b)

Fig. .

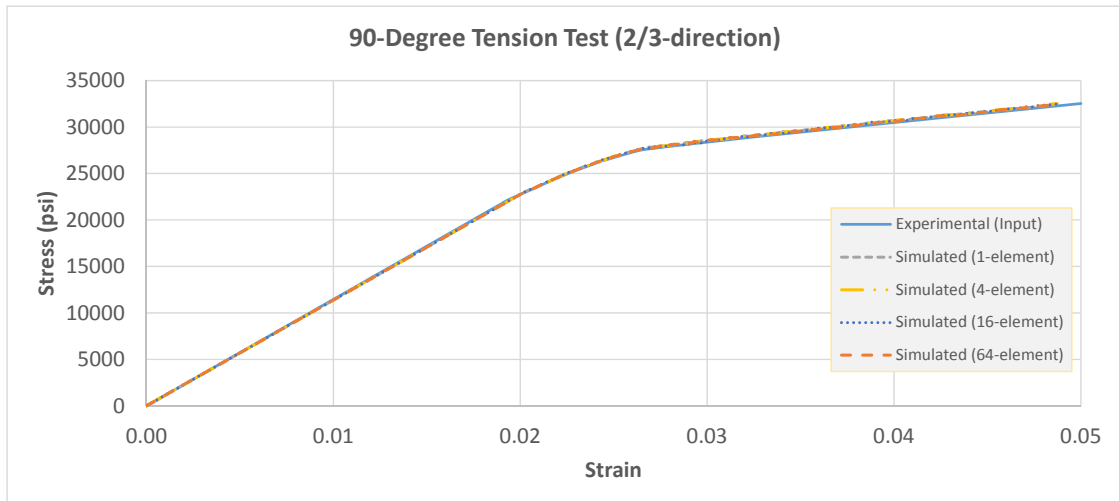


(a)



(b)

Fig. 9. Simulated and experimental stress-strain curves for 1-direction (a) tension and (b) compression



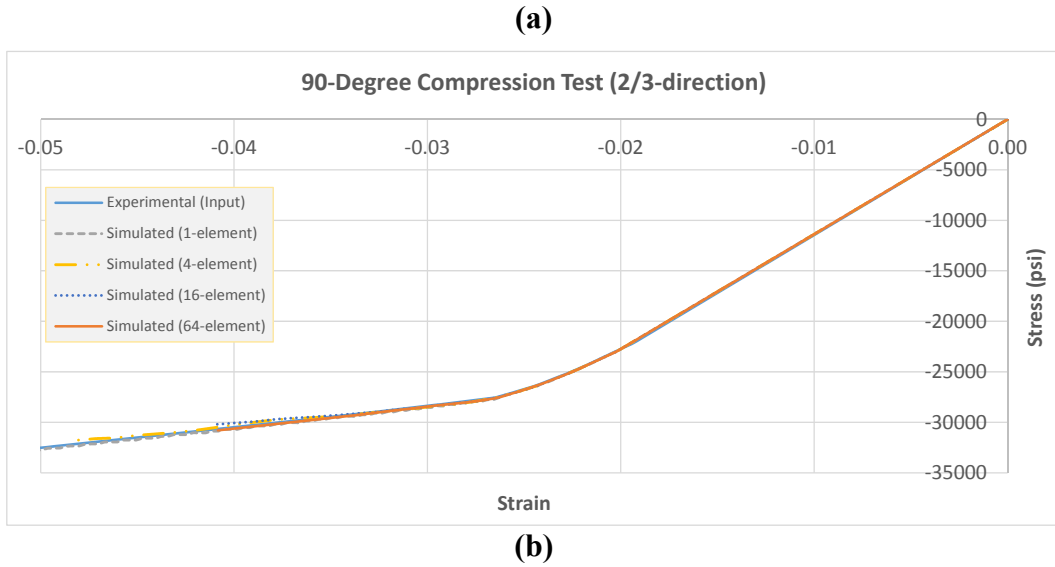


Fig. 10. Simulated and experimental stress-strain curves for 2/3-directions (a) tension and (b) compression

A schematic for the pure shear test is shown in Fig. 11. Nodes on the bottom surface are restrained in the x and y-directions while nodes on the top surface are restrained in the y-direction. A displacement controlled loading of 0.5 in/s in the x-direction is applied to all the nodes on the top surface.

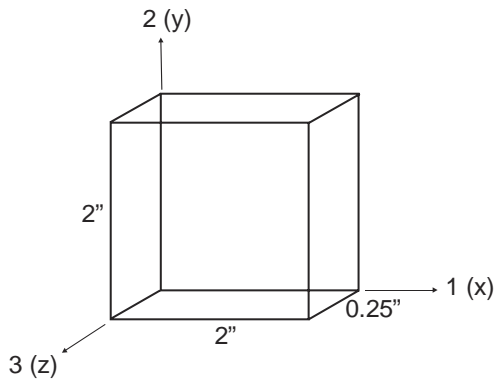


Fig. 11. Schematic for pure shear test in 1-2/3-1 plane

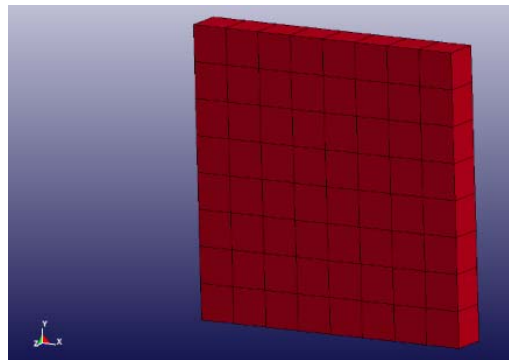


Fig. 12. 64-element mesh for pure shear test cases

The 64-element mesh is shown in Fig. 12. The simulated and experimental stress-strain curves in the 1-2/3-1 plane are shown in Fig. 13 and in the 2-3 plane in Fig. 14.

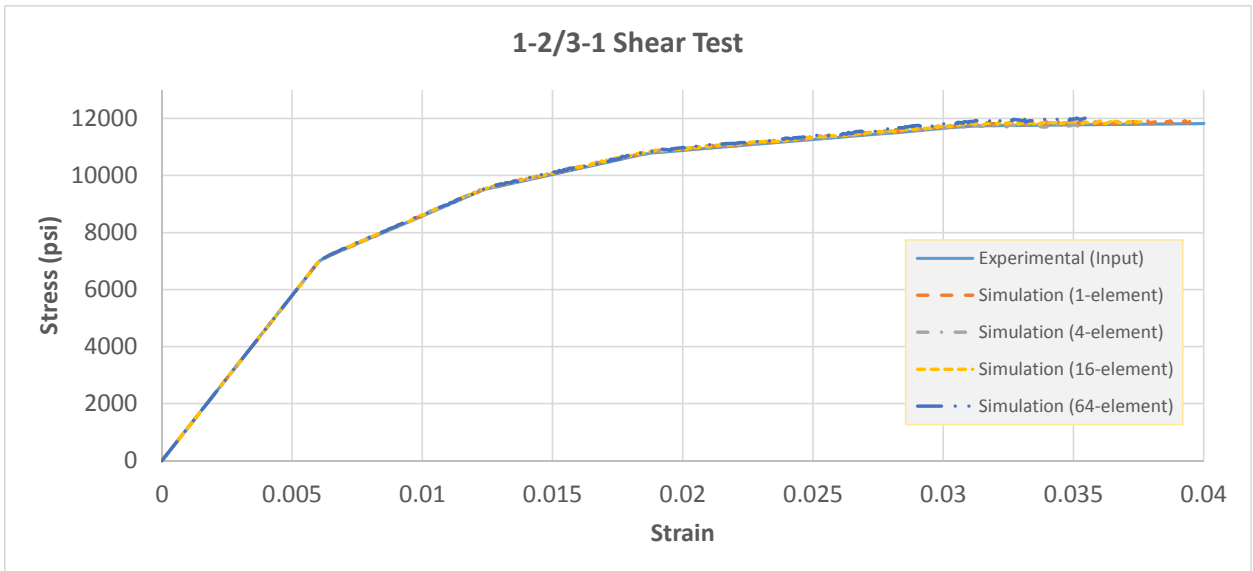


Fig. 13. Simulated and experimental stress-strain curves for pure shear in the 1-2/3-1 plane

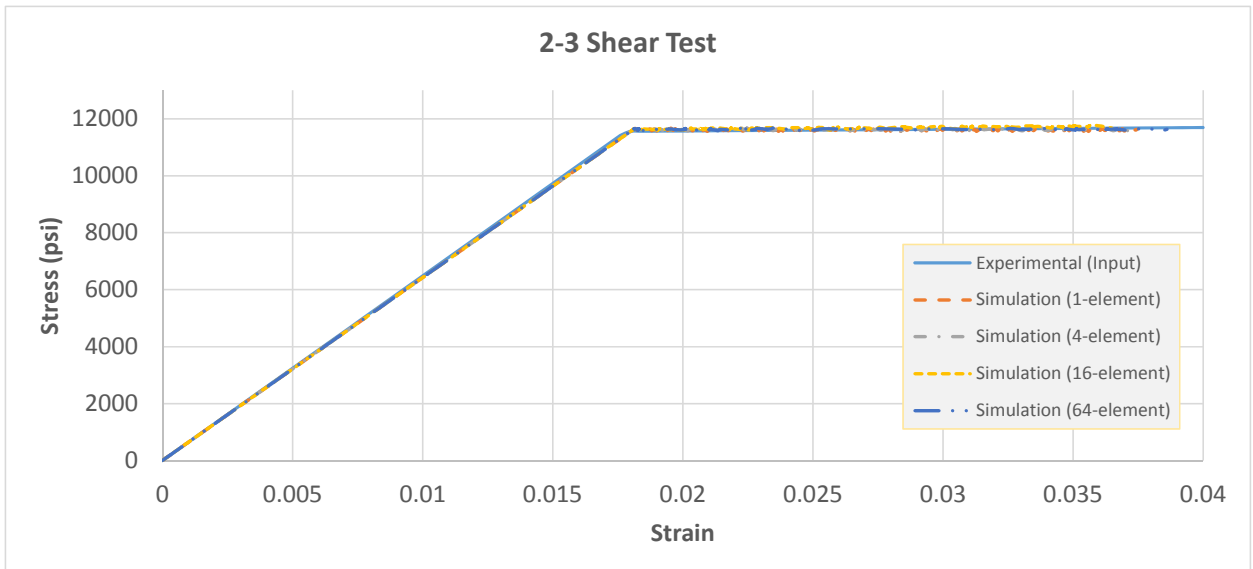


Fig. 14. Simulated and experimental stress-strain curves for pure shear in the 2-3 plane

The (tension) off-axis test model is shown in Fig. 1. Nodes on face ABC were constrained in the x-direction and the center node was also constrained in the y-direction. The simulated and experimental stress-strain curves are compared in Fig. 2, showing very little differences in the results. Finally, Fig. 17 shows the results from a loading-unloading-reloading test case.

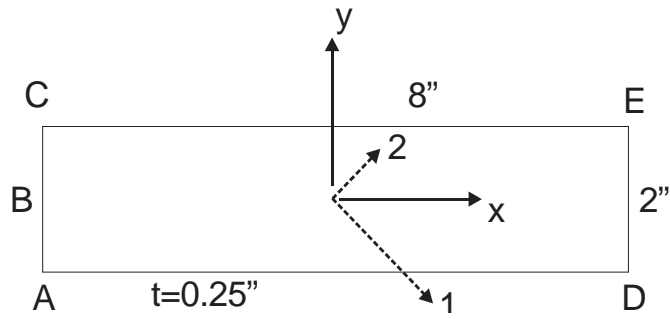


Fig. 1. Schematic for 45° off axis test in 1-2/3-1 plane

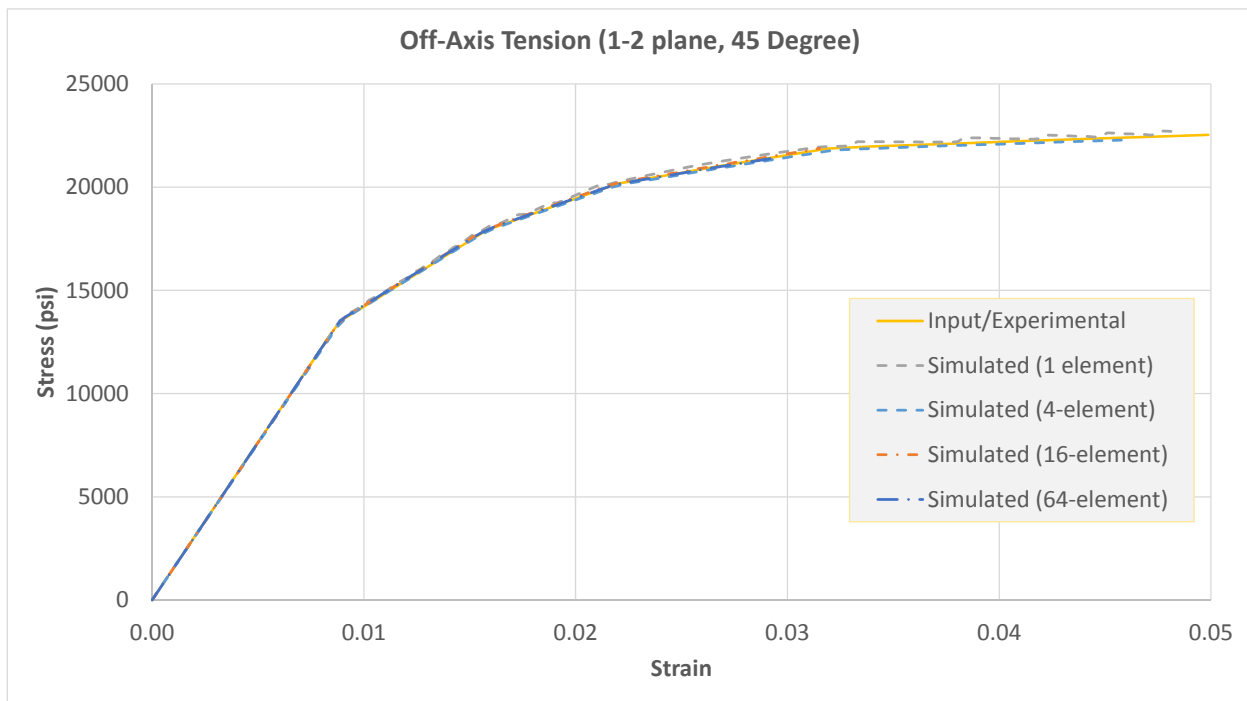


Fig. 2. Simulated and experimental stress-strain curves for 45° off axis test in 1-2/3-1 plane

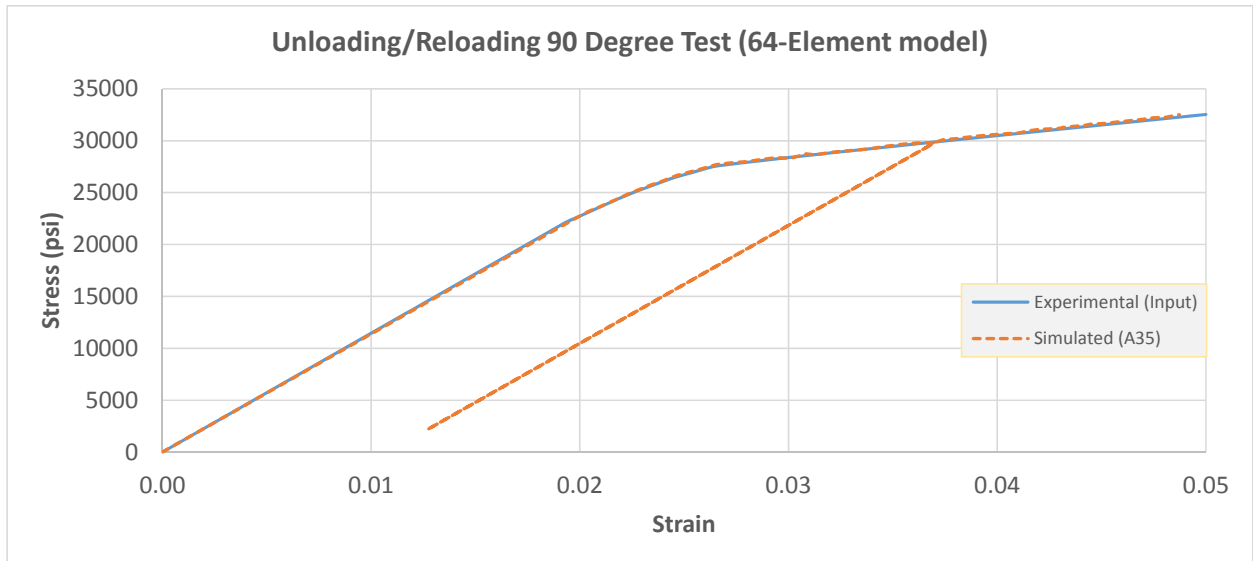


Fig. 3. Simulated and experimental stress-strain curves for unloading/reloading in the 2-direction

Simulations of all the 12 curves as an integral part of the verification process shows very good correlation with the input data. We have used boundary conditions that resemble the experimental test setup as closely as possible so as to capture the actual test conditions. The use of 4 different meshes with increasing mesh density, shows that the results are mesh independent.

Structural Test

To gauge the performance of the implemented constitutive model, a structural test case is designed. A simply-supported 12" long x 2.4" wide x 0.6" thick plate made of T800-F3900 composite material is subjected to an impact from a steel ball. Fig. 4 shows the schematic diagram. The nodes on the bottom of the left edge are constrained in the x, y and z-directions while nodes on the bottom of the right edge were constrained only in the y-direction. In the absence of experimental data, the primary objectives were to ensure that the material model (in the absence of damage and failure) would yield expected results – ball would impact the plate and bounce back, and the peak stresses in the plate would occur around the point of contact immediately after the impact. The LS-DYNA FE model is shown in Fig. 5.

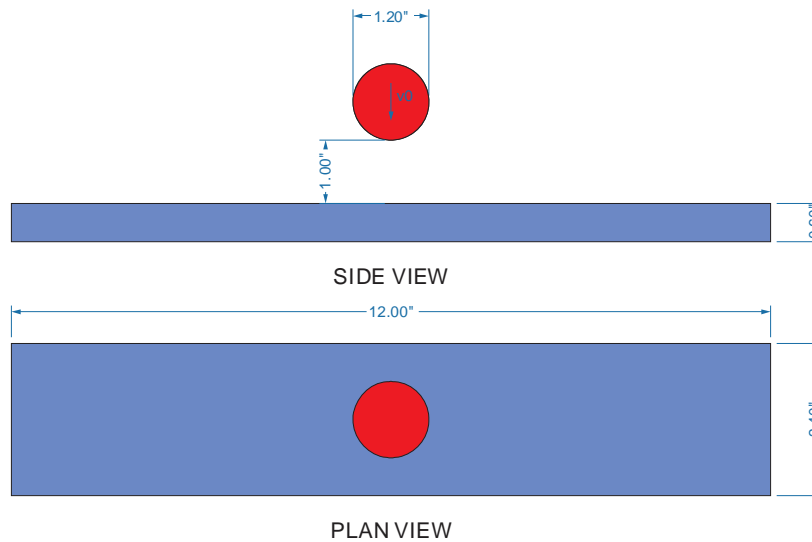


Fig. 4 Schematic diagram of the test

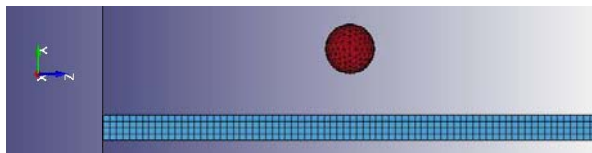


Fig. 5 LS-DYNA FE model at the start of the analysis

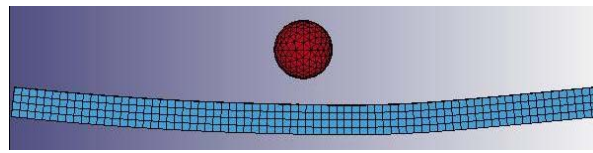


Fig. 20. Deformed model after impact

The model has 6,478 nodes and 5,707 elements of which 1,147 8-noded hexahedral elements are used to model the plate (master surface) and the remaining 4,560 elements are used in the ball (slave surface). The ball is modeled using *MAT_3 and the plate as *MAT_213. *CONTACT_AUTOMATIC_SURFACE_TO_SURFACE is used to describe the contact between the ball and plate. Both the static (f_s) and the dynamic (f_d) coefficients of friction are set to 0.1. A 2% viscous damping coefficient is used. Segment-based contact is used by setting the soft parameter to 2. The steel ball is given a -700 in/s initial velocity in the y-direction. The analysis is carried out for 0.1 seconds. The results are as expected. The exaggerated deformed shape is shown in Fig. 20 just after contact is initiated. The von Mises stress throughout the test duration is plotted for the elements closest to the point of contact in Fig. 21.

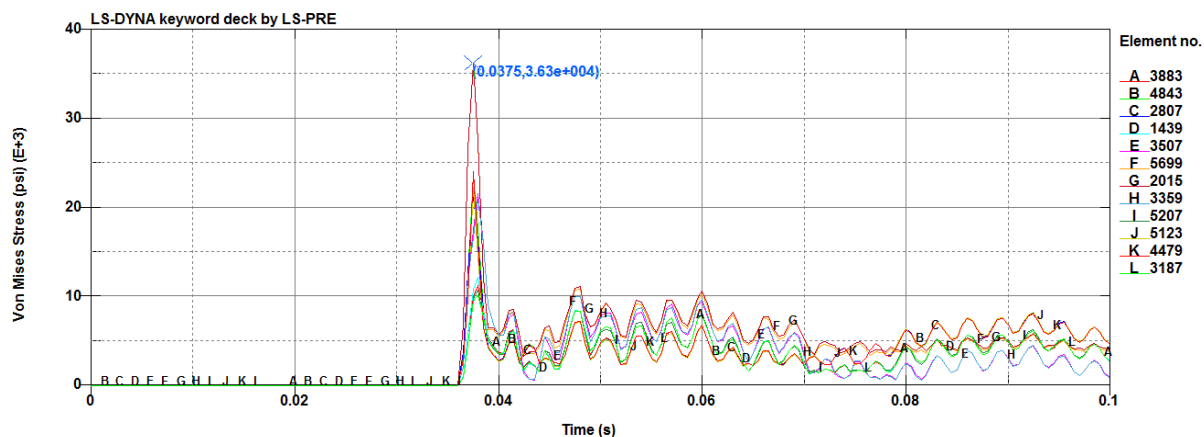


Fig. 21. von Mises stress vs. time for elements near point of impact

Conclusions

A generalized three-dimensional composite material model is developed and verified. The preliminary results are encouraging as the implemented constitutive model is able to reproduce the experimental stress-strain curves. In addition, a simple contact problem involving the composite material yields reasonable results. Future work includes the following – adding damage accumulation and failure in the material model, supporting temperature and strain rate dependent stress-strain curves, using alternate methods to compute the plastic multiplier when the initial yield and flow surface convexity conditions are not met, using a fiber-referenced convected system to track the principal material directions and supporting plate/shell elements.

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